

Transformations Review

Transformations

Type	Key Words	Rules
Translation <u>iso</u>	left, right, up, down	Translation in the x Direction Translation in the y Direction left $x -$ up $y +$ right $x +$ down $y -$
Reflection <u>iso</u>	flip, mirror	X - axis y - axis $y = x$ $y = -x$ (x, y) $(x, -y)$ $(-x, y)$ (y, x) $(-y, -x)$
Rotation <u>iso</u>	"around origin"	90c/270cc 180c/cc 270c/90cc 360c/cc (x, y) $(y, -x)$ $(-x, -y)$ $(-y, x)$ (x, y)
Dilation <u>Nope</u>	stretch	Resulting image is same shape, but <u>not</u> same size

Isometry: Transformation in which the preimage and image are congruent!

Compositions:

Ex1) Describe each algebraic rule by giving the two transformations it describes.

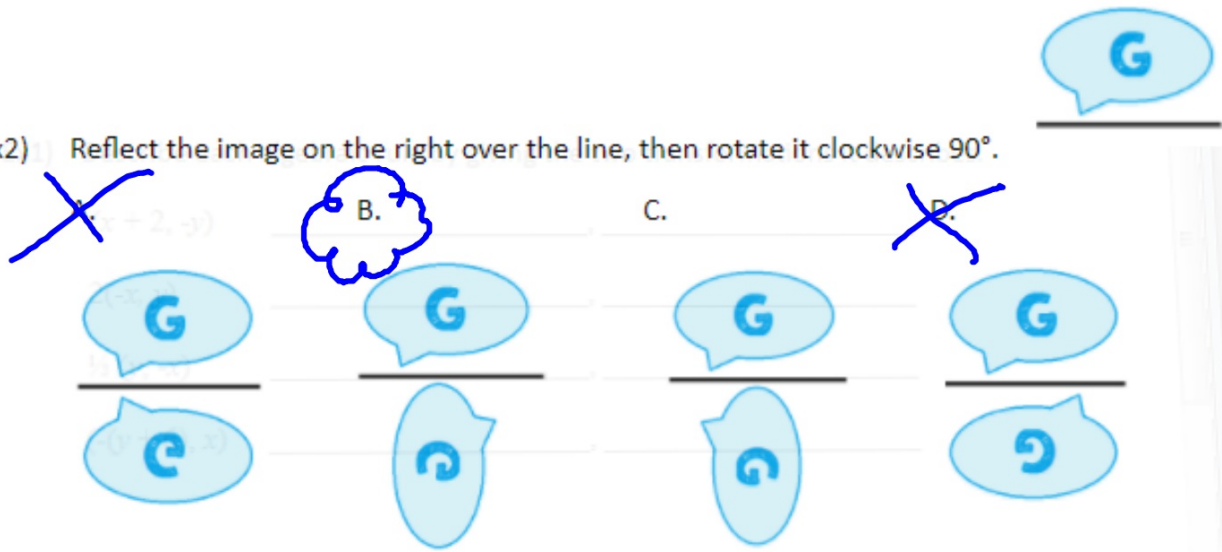
$(x + 2, -y)$ translate right 2. Reflect x-axis

① $2(-x, y)$ dilate by 2. Reflect y-axis

① $\frac{1}{3}(y, -x)$ dilate by $\frac{1}{3}$. Rotate $90^\circ/270^\circ$

$(-(y + 6), x)$ translate up 6. Rotate $270^\circ/90^\circ$

Ex2) Reflect the image on the right over the line, then rotate it clockwise 90°.

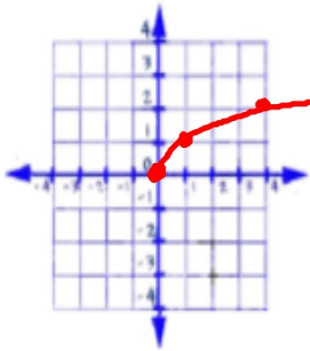


Graphing

Quadratics		
Parent: $y = x^2$	Transformations:	Other Notes:
	$y = a(x-h)^2 + k$ <p>a: stretch/compress (-) reflections</p> <p>h: translate left/right ★ opposite ★</p> <p>k: translate up/down</p>	<p>Writing equations in vertex form: Complete the square!</p> <p>Ex: $y = x^2 - 6x + 10$</p> $\frac{-(-6)}{2} = (-3)^2 = 9$ $y = \underline{(x-3)^2} + \underline{1}$ <p>right 3 up 1</p> <p>"give the bank one"</p>

Square Root Functions

Parent: $y = \sqrt{x}$



Transformations:

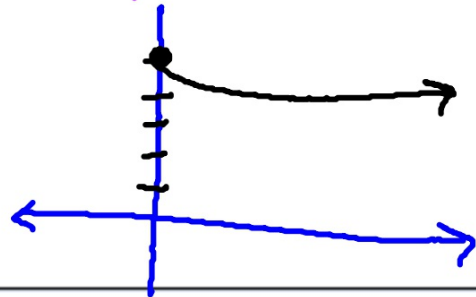
$$y = a\sqrt{x-h} + k$$

* a, h, k
Same as
above

Other Notes:

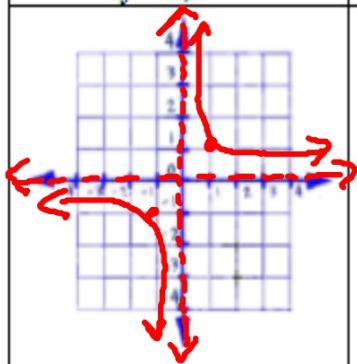
Example: $-\frac{1}{3}\sqrt{x} + 5$

Reflect over x-axis
Compress by $\frac{1}{3}$
up 5



Rational Functions

Parent: $y = 1/x$



Transformations:

$$y = \frac{a}{x-h} + k$$

a, h, k same as above

vertical asymptote $x = h$

horizontal asymptote $y = k$

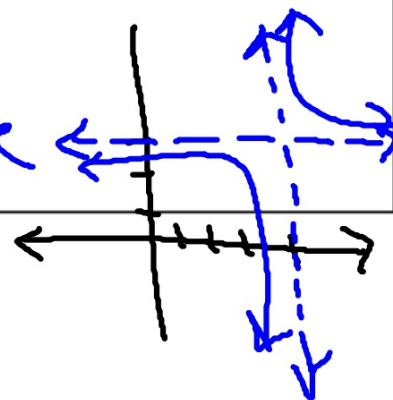
Other Notes:

Example: $y = \frac{1}{x-4} + 3$

Translate right 4, up 3

V.A @ $x = 4$

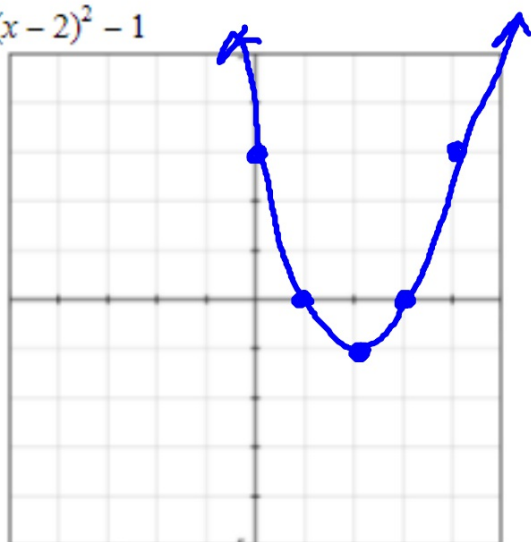
H.A @ $y = 3$



Mixed Review Problems

Graph the Parabola

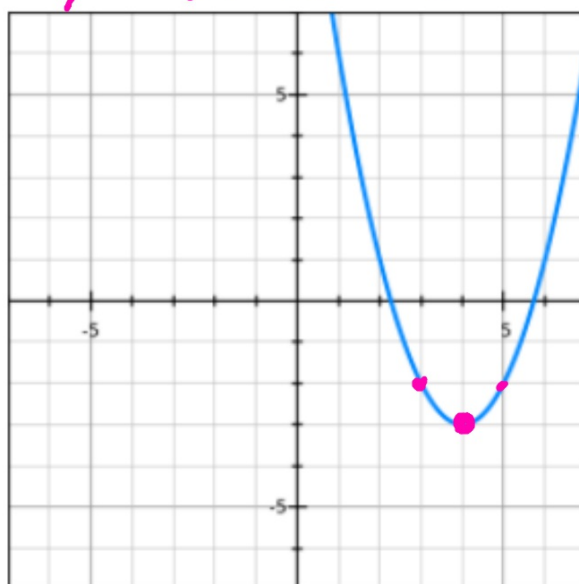
$$y = (x - 2)^2 - 1$$



Right 2
down 1

Write the Equation in Vertex Form

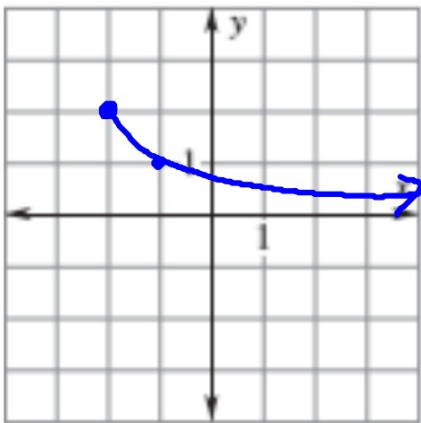
$$y = (x - 4)^2 - 3$$



Right 4, down 3

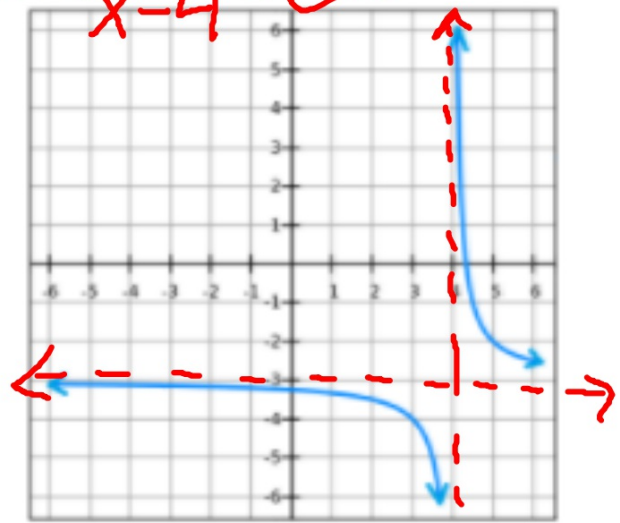
List the transformations and Draw the graph or Write the Equation

$$f(x) = -\sqrt{x+2} + 2$$



Reflect over x-axis
left + 2
up 2

$$y = \frac{1}{x-4} - 3$$



Right 4
down 3