

We now have a remainder of 1, which still has to be divided by $3x - 2$. Thus our final answer now is:

$$\frac{27x^3 + 9x^2 - 3x - 9}{3x - 2} = 9x^2 + 9x + 5 + \frac{1}{3x - 2}$$

Exercises

Use polynomial division to simplify each of the following quotients.

$$\begin{array}{lll} \text{a)} \quad \frac{x^4 + 3x^3 - x^2 - x + 6}{x + 3} & \text{b)} \quad \frac{2x^4 - 5x^3 + 2x^2 + 5x - 10}{x - 2} & \text{c)} \quad \frac{7x^4 - 10x^3 + 3x^2 + 3x - 3}{x - 1} \\ \text{d)} \quad \frac{2x^4 + 8x^3 - 5x^2 - 4x + 2}{x^2 + 4x - 2} & \text{e)} \quad \frac{3x^4 - x^3 + 8x^2 + 5x + 3}{x^2 - x + 3} & \text{f)} \quad \frac{3x^4 + 9x^3 - 5x^2 - 6x + 2}{3x^2 - 2} \\ \text{g)} \quad \frac{x^3 - 2x^2 - 4}{x - 2} & \text{h)} \quad \frac{x^3 - 4x^2 + 9}{x - 3} & \text{i)} \quad \frac{x^4 - 13x - 42}{x^2 - x - 6} \end{array}$$

Answers

$$\begin{array}{lll} \text{a)} \quad x^3 - x + 2 & \text{b)} \quad 2x^3 - x^2 + 5 & \text{c)} \quad 7x^3 - 3x^2 + 3 \\ \text{d)} \quad 2x^2 - 1 & \text{e)} \quad 3x^2 + 2x + 1 & \text{f)} \quad x^2 + 3x - 1 \\ \text{g)} \quad x^2 + 2x + 2 & \text{h)} \quad x^2 - x - 3 & \text{i)} \quad x^2 + x + 7 \end{array}$$